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# Summer Math Skills for 7th Grade going into 8th Grade (Must Show All Work and Attach Scrap paper for Full Credit) 

Copy and complete the statement using <, >, or $=$.

1. 17.1 g ? 1.71 mg
2. $6.3 \mathrm{~cm} \underline{?} 63 \mathrm{~mm}$
3. 1250 mL ? 12.5 kL

Evaluate the expression for the given value(s) of the variables(s).
4. $m-8$ when $m=12$
5. $11 y$ when $y=5$
6. $a \div(b-4)$ when $a=24$ and $b=7$

Evaluate the expression.
7. $23-(9-5)^{2}$
8. $\frac{17-8}{6+12}$
9. $52 \div(13 \times 2)$
10. $-5 \cdot 8 \cdot\left(\frac{1}{5}\right)$
11. $\frac{1}{3}(1.3)+\frac{1}{3}(1.7)$
12. $9^{2}-16 \times 3$
13. $9.83+(8.2)(7.01)$

Find the sum, difference, product, or quotient.
14. $3.24+5.48$
15. $21.73-14.87$
16. $2.4 \times 0.125$
17. $15.3 \div 0.09$
18. $\frac{11}{16}+\frac{3}{4}$
19. $7 \frac{2}{5}-4 \frac{7}{10}$
20. $2 \frac{1}{3} \cdot 3 \frac{3}{4}$
21. $\frac{7}{12} \div \frac{14}{15}$
22. $-11+(-17)$
23. $21-32$
24. $10(-3)$
25. $-54 \div(-6)$

Write the number in scientific notation.
26. 61,500
27. $17,540,000$

Find the mean, median, mode(s), and range of the data.
28. $23,19,32,28,17,21,28$
29. $2.4,1.7,2.1,1.5,2.3,2.1,1.9,1.2$

Use a factor tree to write the prime factorization of the numbers. Then find the GCF and the LCM of the numbers.
30. 45,150
31. 68,102

Write the decimal as a fraction or mixed number. Simplify
32. 0.04
33. 2.35

Order the integers from least to greatest.
34. $-6,3,-4,0,-11,9$
35. $42,-36,17,-28,21,-16$
36. Write the integer that represents a loss of 52 pounds. Then write the opposite of that integer.

Write the verbal sentence as an equation. Let $x$ represent the number.
37. 7 less than a number is 15 .
38. 3 times the sum of a number and 2 is 12 .

Simplify the expression.
39. $4 x-8-7 x-3$
40. $17 t+3(4 t-5)$
41. $5(3 m+1)-8(2 m+3)$
42. $-3-4 b+b-8$

## Solve the equation. Check your solution.

43. $w-4=-2$
44. $\frac{2}{3} x=-10$
45. $4 y-2=7$
46. $-9=-9(2 z-3)$

Solve the inequality.
47. $15>m+8$
48. $-7 x \leq 21$

Solve the proportion.
49. $\frac{x}{15}=\frac{3}{7.5}$
50. $\frac{12}{16}=\frac{y}{12}$
51. A map uses a scale of $1 \mathrm{in} .: 25 \mathrm{mi}$. If the distance between two cities on the map is 3.5 inches, what is the actual distance between the cities?

Write the percent as a decimal or the decimal as a percent.
52. 31.5\%
53. $210 \%$
54. 0.0125
55. What number is $45 \%$ of 520 ?
56. 75 is what percent of 30 ?

Identify the percent of change as an increase or a decrease. Then find the percent of change.
57. Original: 60

New: 45
58. Original: 75

New: 90
59. A store has a pair of boots that originally cost $\$ 56$ marked down $25 \%$. How much will the boots cost on sale?
60. You deposit $\$ 1200$ in an account. The annual interest rate is $3 \%$. How long will it take you to earn $\$ 108$ in simple interest?

Use the diagram to find the unknown angle measures.

61. $m \angle 1$
62. $m \angle 2$
63. $m \angle 3$

Classify the triangle by its side lengths.
64. 5, 5, 5
65. 7, 3, 5
66. Given that $\Delta E F G \cong \Delta H I J$, name the corresponding sides and corresponding angles.
67. Find the unknown length given that the triangles are similar.

68. The shadow cast by a house is 55 feet long. At the same time, a flagpole that is 15 feet tall casts a 25 foot long shadow. How tall is the house?

Evaluate the expression when $x=3$ and $y=15$.
69. $-\sqrt{12 x}$
70. $\sqrt{y-2 x+7}$

## Solve the equation.

71. $a^{2}-16=48$
72. $3 b^{2}-7=68$
73. $15+c=-3$
74. $\frac{3}{4} x=12$
75. $4+t^{2}=68$

Find the unknown length. (Hint: Pythagorean Theorem)
Round to the nearest tenth if necessary.
76.

77.


Use the following information. A bag contains the letters from the words SUMMER VACATION. (Refers to questions 102, 103, and 104)
78. You randomly choose a letter. What is the probability that you choose the letter M?
79. You randomly choose a letter C, replace it, and then choose a letter M. What is the probability of this happening?
80. You randomly choose a letter A, and do not replace it. Then you choose another letter A. What is the probability that both letters are A's?

## Graph the function.

81. $y=.5 x$

82. $y=-3 x+1$


Evaluate the expression for the given value of the variable.
83. $12-x+7$, when $x=5$
84. A rectangular garden has a length of 10.25 feet and a width of 6.2 feet. Another rectangular garden has a length of 20.5 feet and a width of 12.4 feet. How many times greater is the area of the larger garden than the area of the smaller garden?

Find the quotient.
85. Evaluate the expression $\left(\frac{1}{2}\right)^{2} \div \frac{2}{3}$.

Evaluate the expression when $a=-5, b=7, c=-2$, and $d=3.2$.
86. $a^{2}-b+(4.7-d)-c$

Find the unit rate.
87. $\frac{\$ 18}{4 \text { people }}$

## Solve the following proportion problem.

88. You can walk 2 miles in 24 minutes. How long will it take you to walk 5 miles?
89. In the jazz band, 8 out of 24 students are in eighth grade. What percent of the students are not in eighth grade?
90. Your bill at a restaurant comes to $\$ 56$. You want to leave a $15 \%$ tip. How much should you leave?

Find the area of the figure.


Find the unknown length. (Hint: Pythagorean Theorem)
92.


Find the circumference and area of the circle. Use $\mathbf{3 . 1 4}$ for $\pi$.
93.

94. Make a line graph of the number of bald eagles at a national wildlife reserve.

| Year | 1997 | 1998 | 1999 | 2000 | 2001 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Eagles | 6 | 8 | 17 | 14 | 20 |



Solve the inequality. Then graph its solution.
95. $x-4>15$
96. $6 x-8<-20$
a. $\quad x>-2$

c. $x>2$

b. $x<-2$
d. $x<2$

97. $-\frac{x}{7} \leq 8$

98. $\frac{x}{9}<-9$


Write a function rule for the input-output table. Then graph the function.
99.

| Input, $x$ | 1 | 2 | 3 | 4 |
| :--- | :---: | :---: | :---: | :---: |
| Output, $y$ | 3 | 6 | 9 | 12 |



Draw the graph of the line that passes through the two points. Then find the slope of the line.
100.


Evaluate the expression when $a=-6, b=-13$ and $c=4$.
101. $-13+c+b$
a. -15
b. -22
c. -1
d. 1
102. $c+b$
103. $a+(-5)+b$
104. Susan owns a small business. There was a loss of $\$ 11$ on Monday and a profit of $\$ 18$ on Tuesday. On Wednesday, there was a loss of $\$ 7$ and on Thursday, there was a profit of $\$ 8$. Find the total profit or loss.
a. $\$ 13$ loss
b. $\$ 8$ profit
c. $\$ 44$ profit
d. $\$ 18$ profit
105. The Badgers played football against the Raiders. The Badgers had a gain of 7 yards on their first play and a loss of 15 yards on their second play. On the third play there was a loss of 18 yards. Find the total gain or loss for the 3 plays.

Find the difference.
106. $-26-(-9)$
107. $-24-(-10)$

Find the change in temperature.
108. From $-13^{\circ} \mathrm{C}$ to $15^{\circ} \mathrm{C}$.
a. $-28^{\circ} \mathrm{C}$
b. $-2^{\circ} \mathrm{C}$
c. $28^{\circ} \mathrm{C}$
d. $\quad 2^{\circ} \mathrm{C}$
109. From $-1^{\circ} \mathrm{F}$ to $-20^{\circ} \mathrm{F}$.

Evaluate the expression when $x=-4, y=10$, and $z=-9$.
110. $x-y-z$
a. -5
b. -23
c. 15
d. 24
111. $-5-x-z$

Evaluate the expression for the given values of the variables.
112. $-c-p$, when $c=-33$ and $p=20$

Find the product.
113. $-2(-16)$
114. $-7(3)(-1)$

Find the quotient.
115. $-272 \div(-8)$

Evaluate the expression.
116. $\frac{x}{y}$, when $x=-72$ and $y=-2$
117. A deep-sea diver must descend and ascend in short steps to equalize pressure on her body. If the diver rises toward the surface too quickly, she may suffer from a physical condition called "the bends." Suppose the diver descends to the bottom in three steps of 12 feet each. Write and simplify an expression to describe the diver's change in elevation.

Use the distributive property and mental math to find the product.
118. 7(6.1)
a. 427
b. 43.4
c. 4.27
d. 42.7
119. $4(51)$
120. Kaye runs a small business with three employees. She pays one employee $\$ 2300$ a month, another $\$ 1700$ a month, and the third $\$ 1400$ a month. How much does she pay her employees in a year?
a. $\$ 31,900$
b. $\$ 63,600$
c. $\$ 30,700$
d. $\$ 64,800$

Use the distributive property to write an equivalent variable expression.
121. $4(x+3)$
a. $4 x+12$
b. $4 x-12$
c. $4 x+3$
d. $7 x+3$
122. $3(3-7 x)$
123. You and three friends go to a movie. The tickets cost $\$ 5.50$ each. You each buy a drink for $\$ 2.50$ and a box of popcorn for $\$ 4.00$. Write an expression that represents the total amount of money spent. Then evaluate the expression.
124. $-4(x+3)$
125. Consider the rectangle shown.

a. Write an expression for the area of the rectangle.
b. Find the area for $x=2$.

Identify the terms, like terms, coefficients, and constant terms. Then simplify the expression.
126. $3 n-13-5 n+6 n$

## Simplify the expression.

127. $7-7(5+x)-9 x$
128. $4+10 x+5-9 x$
129. Write and simplify an expression for the perimeter of the figure. (The figure may not be drawn to scale.)


Solve the equation. Check your solution.
130. $s-45=127$
131. $164=x-59$
132. The perimeter of the triangle is 131 inches. Write an equation to find the side length labeled $x$. Then solve the equation.


Solve the equation.
133. $14 x=-728$
a. $-\frac{1}{52}$
b. $\frac{1}{52}$
c. 52
d. -52
134. $\frac{t}{3}=9$
135. $7 x=182$
136. $\frac{e}{4}=23$
137. $4 x=24$
138. $\frac{c}{24}=19$
139. You receive $\$ 68$ for mowing lawns for 8 hours. What equation can you use to find how much you make per hour?
a. none of these
b. $68 x=8$
c. $\frac{x}{8}=68$
d. $8 x=68$
140. A person-hour is a unit of measure representing one person working for one hour. A construction foreman estimates that it will take 2880 person-hours to build a new library. If 12 workers are scheduled to work on the project at the same time, how many hours will it take to complete the project?

Perform the indicated operation.
141. $-8(2.25)$

Solve the equation.
142. $1.87=x+11.04$
143. The perimeter of the figure is 28.01 centimeters. Find the value of $x$.


## Solve the equation. Check your solution.

144. $-x+6=8$
145. $-\frac{q}{4}+3=18$
146. $\frac{t}{14}+9=13$
147. $-\frac{w}{7}-2=19$
148. The vice-president of a bank earns $\$ 1635$ per week. This is $\$ 55$ more than two times the weekly wage of a bank manager. Write an equation and a solution that show the weekly wage of a bank manager.
a. $\quad 1635=2 x+55 ; \$ 790$
c. $1635=55-2 x ; \$ 780$
b. $1635=2 x-55 ; \$ 845$
d. none of these

Solve the equation.
149. $2(2 x-3)=x+7$
150. $3(x+5)+1=2(x+5)+4$
151. $x+6=5(3 x-1)$
152. $11-2 x=5 x-12$

Write the verbal sentence as an equation. Then solve the equation.
153. Fifteen plus twice a number is equal to 3 times the number.
a. $15+2 x=3 x ; 15$
c. $15=2 x+3 x ; 3$
b. $\quad 15+3 x=2 x ;-1$
d. none of these
154. Eighteen minus 8 times a number is equal to -6 times the number.
155. Find the value of $x$ so that the rectangle and the triangle have the same perimeter. What is the perimeter?

156. Find the value of $x$ so that the figure is a square.


Solve the inequality. Then graph the solution.
157. $-4 x+10>2$

158. $7-\frac{x}{5}<27$
159. $\frac{m}{2}+1 \geq-1$
160. The width of a rectangle is 21 centimeters. The perimeter is at least 316 centimeters. Write an inequality that represents all possible values for the length of the rectangle. Then solve the inequality.
161. Write the prime factorization of 55 .
a. $5^{2} \cdot 11^{2}$
b. $5^{2} \cdot 11$
c. $5 \cdot 11$
d. $5 \cdot 11^{2}$
162. Write $56 k^{2} l^{3}$ in factored form.
a. $\quad 2 \cdot 2 \cdot 2 \cdot 7 \cdot k \cdot k \cdot l \cdot l$
b. $2 \cdot 2 \cdot 2 \cdot 7 \cdot k \cdot k \cdot l \cdot l \cdot l$
c. $2 \cdot 2 \cdot 2 \cdot 7 \cdot k \cdot k \cdot k \cdot l \cdot l \cdot l$
d. $2 \cdot 2 \cdot 7 \cdot k \cdot k \cdot l \cdot l \cdot l$
163. Make a factor tree for 420 .

Write the prime factorization of the number.
164. 336

## Factor the monomial.

165. $27 n^{2} o$

Find the greatest common factor of the numbers.
166. 72,96
a. 144
b. 3
c. 24
d. 13
167. $30,20,40$

Find the greatest common factor of the monomials.
168. $108 a^{4} b^{3}, 64 a^{3} b$
a. $4 a^{4} b^{3}$
b. $4 a^{3} b$
c. $2 a^{3} b$
d. $4 a^{3} b^{3}$
169. $15 f^{6} g^{5}, 60 f^{2} g^{8}$

Find the least common multiple of the numbers.
170. $3,15,33$
a. 99
b. 3
c. 165
d. 495

Find the least common multiple of the monomials.
171. $10 u v, 6 u^{2}$
a. $\quad 30 u^{2} v$
b. $\quad 15 u^{2} v$
c. $2 u$
d. $30 u v$
172. $4 x^{3} y z^{2}, 18 x y^{5} z$
a. $\quad 36 x^{3} y^{5} z^{2}$
b. $72 x^{4} y^{6} z^{3}$
c. $36 x^{4} y^{6} z^{3}$
d. $72 x^{3} y^{5} z^{2}$
173. $12 c^{3} d^{4}, 7 c^{4} d^{5}$

Find the missing exponent.
174. $4^{?} \cdot 4^{3}=4^{12}$
a. 15
b. 9
c. 4
d. 2
175. $\frac{15^{?}}{15^{2}}=15^{3}$

Find the product. Write your answer using exponents.
176. $3^{4} \cdot 3^{7}$
a. $3^{28}$
b. $9^{28}$
c. $9^{11}$
d. $3^{11}$

Simplify the expression. Write your answer using exponents.
177. $\frac{t^{15}}{t^{13}}$
a. $t^{2}$
c. $t^{28}$
b. $t^{195}$
d. none of these
178. $p^{11} \cdot p^{5}$

Simplify the expression.
179. $2 a^{2} b^{5} \cdot 6 a^{9} b^{3}$
a. $\quad 8 a^{11} b^{8}$
b. $8 a^{8} b^{11}$
c. $12 a^{18} b^{15}$
d. $12 a^{11} b^{8}$
180. $\frac{m^{9} p^{16}}{m^{3} p^{12}}$
a. $\frac{1}{m^{6} p^{4}}$
b. $m^{6} p^{4}$
c. $m^{12} p^{28}$
d. $m p^{4}$
181. $3 g^{6} \cdot 3^{3} g^{9}$
182. $\frac{5 x^{7} y^{8} \cdot 6 x y^{3}}{3 x^{2} y}$

Copy and complete the statement using $<,>$, or $=$.
183. $5^{4}-5^{3} \cdot 5^{2}$
184. $7^{9}-7^{7} \cdot 7^{2}$

Find the sum or difference.
185. $6 \frac{1}{4}-3 \frac{1}{6}$
a. $2 \frac{1}{12}$
b. $3 \frac{1}{12}$
c. 4
d. $4 \frac{1}{24}$
186. $9 \frac{2}{3}+8 \frac{3}{8}$
187. $\frac{1}{5}+\frac{6}{20}$

Evaluate the expression when $x=\frac{2}{7}$ and $y=-\frac{3}{4}$.
188. $x-y$
a. $-\frac{13}{28}$
b. $1 \frac{2}{3}$
c. $\frac{5}{11}$
d. $\quad 1 \frac{1}{28}$
189. $y+x$
a. $\frac{13}{28}$
b. $\frac{1}{28}$
c. $-\frac{13}{28}$
d. $\frac{5}{28}$

Evaluate the expression.
190. $-5 \frac{2}{3}+\frac{1}{9}-\frac{15}{18}$

Solve the equation. Check your solution.
191. $50=\frac{5}{2} x$
a. 25
b. 125
c. 20
d. 10
192. $-\frac{2}{7} x=36$
a. 126
b. $10 \frac{2}{7}$
c. -126
d. $-10 \frac{2}{7}$
193. $\frac{1}{2} y-2=4$
194. $\frac{9}{10} g=\frac{5}{9}$
195. $2 \frac{1}{3} t-22=41$

Use the percent equation to answer the question.
196. 12 is $20 \%$ of what number?
197. What percent of 25 is 7 ?
198. What number is $21 \%$ of 300 ?
199. Luis makes a $4 \%$ commission on his sales in a sporting goods store. For a $\$ 70$ purchase, how much commission does Luis earn?

Identify the percent of change as an increase or a decrease. Then find the percent of change. Round your answer to the nearest tenth if necessary.
200. Original: 236

New: 223
201. Original: 276

New: 296

Find the new amount.
$\qquad$ 202. Increase 30 by $80 \%$.
a. 6
b. 54
c. 24
d. 110
203. Decrease 40 by $20 \%$.
a. 20
b. 32
c. 8
d. 48
204. The table shows the number of guests at Bonnie's Bed and Breakfast for several years. What was the percent increase from 1992 to 1994 ? Round your answer to the nearest whole percent.

| Year | 1991 | 1992 | 1993 | 1994 |
| :--- | :---: | :---: | :---: | :---: |
| Guests | 310 | 349 | 407 | 481 |

205. The table shows the revenue of a local automobile dealership. Find the percent of increase in the revenue from 1998 to 2001. Round to the nearest tenth of a percent.

| Year | Revenue |
| :---: | :---: |
| 1992 | 95,000 |
| 1996 | 145,000 |
| 1998 | 105,000 |
| 2001 | 315,000 |

Solve the equation. Check your answer.
206. $11 x-2=75$
a. 73
b. 7
c. 4
d. 16
207. $4 m+7=35$
a. 10.5
b. 112
c. 7
d. 168

Solve the equation. Check your answer.
208. $\frac{r}{4}+14=46$
a. 16,015
b. 240
c. 8
d. 128
209. $\frac{w}{7}-4=9$
210. Which inequality is represented by the graph?

a. $m \leq-12$
b. $m>-12$
c. $m \geq-12$
d. $m<-12$

Solve the inequality. Then graph its solution.
211. $x-28 \leq-9$
212. $x-4 \leq 0.9$

213. $w+8 \leq 18$

214. $w+\frac{3}{2}<3$


Write the inequality for the following sentence.
215. A number decreased by 7 is more than 3 .

Write a verbal phrase to describe the inequality. Then graph the inequality on a number line.
216. $m \geq 6$

217. Find the mean of the integers.
$44,63,-17,28,-30,-24,19,51,-8$
218. During the hockey season, Pete scored goals on $15 \%$ of the shots he took. If he scored 75 goals, how many shots did he take?
a. 113
b. 1125
c. 50
d. 500
219. What is a salesperson's commission on a $\$ 1000$ sale if the commission rate is $20 \%$ ?
a. $\$ 20,000$
b. $\$ 1020$
c. $\$ 200$
d. $\$ 20$
220. A man buys 12 shirts at $\$ 24.69$ each. There is also a $6 \%$ sales tax. Find his total bill.
221. The sales tax rate in a certain state is $5 \%$. Find the total price paid for a pair of shoes that costs $\$ 39$.
222. You and three friends share a meal at a restaurant. The bill, including $5 \%$ sales tax, comes to $\$ 34.02$.
a. How much is the food bill before sales tax? What was your portion of the food bill?
b. You and your friends decide to leave a $20 \%$ tip. How much does each person need to leave for the tip?
c. One of your friends says that each person needs to leave a total of $\$ 9.72$. Explain why this amount is incorrect.
d. What is the total cost of the meal including the tip?

## Use the given information to find the new amount.

223. Original price: $\$ 15$

Discount percent: 30\%
a. $\quad \$ 19.50$
b. $\$ 10.50$
c. $\$ 4.50$
d. $\$ 14.55$
224. You have $\$ 40.00$. You wish to buy a T-shirt costing $\$ 14.50$ and a pair of jeans costing $\$ 23.95$. There is a $4 \%$ sales tax on clothing. Do you have enough money to pay for both?
225. You have $\$ 40.00$. You wish to buy a T-shirt costing $\$ 14.50$. You would also like to buy a pair of jeans. There is a $6 \%$ sales tax on clothing. What is the top tag price (excludes sales tax) you could pay for the jeans?

